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Object Kinetic Monte Carlo simulation of hydrogen clustering behaviour with vacancies in tungsten

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Abstract. We apply the Object Kinetic Monte Carlo method to simulate the hydrogen (H) clustering behaviour with large vacancy (V) clusters in tungsten. The main advantage of this method is to consider the temperature effects, large V clusters, and long-time evolution. It is thus a very useful tool to study the microstructure evolution of defects in irradiated materials covering from atomic scale to mesoscale. Simulation results show that the number of trapped H atoms by V and V clusters decreases with the increase of temperature. This is expected, because the de-trapping ability of H atoms increases when the temperature is increased. With the correction of the zero-point-energy in calculating binding energies, the present results show that the number of H atoms trapped by monovacancy decreases for all studied temperatures. We also found that the trapping ability of V clusters for H decreases with the increase of the sizes of V clusters, independent on temperature. The H concentration can largely affect the clustering behaviour of H_mV_n . When the H saturation concentration is reached, the clustering behaviour of H_mV_n is mainly determined by the sizes of V clusters.

Keywords: OKMC, hydrogen, vacancy clusters, tungsten

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1. Introduction

Tungsten (W), because of its high melting point, thermal conductivity, and sputtering resistance, is one of the most promising candidates of plasma facing materials (PFM) for future fusion reactors such as International Thermonuclear Experimental Reactor (ITER) [1,2]. During the operation of the fusion reactor, W will be exposed to the low-energy (<100 eV), high-flux (>10²⁴/m²s) hydrogen (H) and helium plasma irradiation, as well as a continuous bombardment of 14.1 MeV neutrons escaped from nuclear fusion reactions [3]. The plasma irradiation on the PFM can lead to the accumulation of H atoms and their isotopes in it. The escaped high energy neutrons colliding with W lattice atoms can cause the displacement of atoms along their paths and create Frenkel pairs of self-interstitial atoms (SIAs) and vacancies in the materials. The continuous creation of vacancies or vacancy clusters (V_n, where n is the number of vacancies) in W under irradiation can serve as traps for H and its isotopes. This was experimentally confirmed by using the thermal desorption spectroscopy (TDS) [4,5]. High retention of H isotopes in W can significantly degrade the fueling efficiency of burning plasmas and thus bing the severe safety concern of reactors. Therefore, it is essential to understand and control the behaviour of H isotopes in irradiated W such as the clustering of H isotopes with vacancy defects.

Simulation approaches are effective tools that can be used to understand the properties of materials. Many researchers have already performed atomic simulations on the microscopic interaction mechanism of H with irradiated defects in W. By using the Density Functional Theory (DFT) method, Qin et al. [6] found that vacancies are very easily formed near the vicinity of H atoms. Liu et al. [7] studied the clustering of H to vacancies and pointed out that a monovacancy can provide a low-density region of electrons, which decreases the binding energy of H to V₁ suggesting that H atoms can be easily trapped by V₁. Results showed that a V₁ can accommodate up to 10 H atoms. Later on, by taking the zero-point energy (ZPE) into account in the calculation of binding energies, Sun et al. [8] showed that a V₁ can trap up to 12 H atoms. Recently, Valles et al. [9] calculated the binding energies of H with both V₁ and V clusters with a number of V up to 4 in order to study the effect of grain boundaries on the defect revolution and H retention in W. Besides the DFT method, the molecular statics (MS) based on empirical potentials is another way to study the clustering behaviour of atoms. Using the MS method, Wang et al. [10] systematically investigated the interaction of H with V clusters containing up to 10 vacancies (V_{10}) by using a newly developed embedded-atom method (EAM) potential. More recently, owing to the genetic algorithm (GA), they can further increase the number of vacancies up to 40 (V_{40}) [11]. The energetically favorable diffusion path for a single H atom in bulk W is from a tetrahedral interstitial site (TIS) to another TIS. The diffusion barrier is 0.20 eV [12]. It was shown in Ref. [7] that the diffusion barrier reduces when a V is present. For the case of a single V trapping multiple H atoms, the diffusion barrier for the first 6 H atoms moving from the 1NN to the stable positions nearby is only 0.02 eV, and 0.18 eV for the 7th H atom, which is lower than that in the bulk. However, atomic simulations are limited by the time and space scales and MS simulations are performed at temperature 0 K. These simulations may not reflect the real clustering behaviour of H and large V clusters at large scale and high operation temperatures.

Object Kinetic Monte Carlo (OKMC) is a very important simulation method. It uses activation energies obtained at the atomistic scale to study the evolution of defects at large scale. Yang et al. [13,14] studied the diffusion coefficients of H atom in both pure W and a reconstructed (0 0 1) W surface using OKMC. A very good agreement between the OKMC results and experimental data was achieved. Oda et al. [15] studied the effect of a V_1 on the diffusion coefficient of H in W. They successfully reproduced the experimental results of H diffusivity. G. Valles et al. [9] investigated the H retention in W with their own OKMC code. Castin et al. studied the microstructural evolution of W under low-dose neutron irradiation using the OKMC model [16]. Their results suggested that the size and density of voids as a function of irradiation dose and temperature were consistent with experimental observations [16]. In another study by Castin et al., they incorporated the effects of the transmutation element of Re and interstitials of W and C on the microstructural evolution in their OKMC model. The model gave a realistic prediction for the formation of nanovoids and TEM-visible SIA loops under neutron or highenergy ion irradiation conditions. The transmuted Re atoms also affect the dislocation loops greatly through a complicated transmutation-diffusion-segregation mechanism [17]. Meng et al. [18] studied the clustering behaviour of H with monovacancies using their own OKMC code, and the temperature dependence of dominating H_mV_1 clusters was obtained. As shown above, although some work on the clustering of H with V has already been done, the temperature-dependent clustering behaviour of H and large V clusters for a long-time evolution in W remains unclear.

In this work, we systematically investigate the clustering behaviour of H with V clusters in W using the OKMC method and our own code, which has been previously validated by studying the behavior of H clustering with monovacancies [18]. We should mention that SIAs are not considered in the simulation although SIAs and vacancies are generated as Frankel pairs after a cascade during the irradiation. The reseaons can be explained in two aspects: firtly, the interaction of SIAs with H atoms can be neglected. C. S. Becquart et al. [19] showed that the calculated binding energy of SIA and H is 0.33 eV, which indicates that the interaction of SIA with H is relatively weak comparing with the H migration with an energy of 0.20 eV especially at the temperature range used in our simulations. Thus, the interaction of H with SIA can be neglected. Secondly, for the interaction of SIAs with vacancy defects, it is believed that the presence of SIAs can affect the clustering behaviour of vacancies. However, in our simulation, we study a bulk case without the presence of any sinks. The SIAs can't be annihiliated in the entire simulation and their migration events will be always selected between cascades in the MC simulation due to its very low migration energy of 0.013 eV [19]. These migration events of SIAs doesn't bring much useful information except significantly increasing the simulation time [17]. To avoid these time consuming migration events of SIAs, our simulation starts from the stage where fastmoving SIAs are assumed to be already annihilated by sinks after a cascade, and those sinks are not explicitly included in our simulation. Therefore, we studied a simple case in which we mainly focus on the clustering behaviours of H and vacancy defects in the bulk W. The effects of temperature, V size, and the initial H concentration on the clustering behaviour of a single H with V clusters in W were thoroughly investigated.

2. Computational method

In this section, we first present the algorithms of the OKMC simulation approach. Then the parameters in the OKMC model for describing the properties of H, V, and their clusters are detailed.

2.1. The Object Kinetic Monte Carlo model

In the OKMC model, various configurations of defects are represented by different states in the system and the transitions between these states follows the Transition State Theory (TST), that is, the transition rates of different states depend on the initial and final states, and are independent on the time. More precisely, in our approach (and many OKMC models), we use the Harmonic Transition State Theory, as a particular TST. The corresponding possibility of transition is assumed to follow an Arrhenius law with an activation energy E_a and a pre-factor P_0 [20] expressed by

$$P = P_0 \times e^{\frac{E_a}{k_B T}} , \qquad (1)$$

where k_B and *T* is the Boltzmann constant and the absolute temperature, respectively. The time increment is acquired by the residence time algorithm (RTA) [21] known as

$$\Delta t = \frac{-\ln(r)}{\sum P} , \qquad (2)$$

where r is a random number between 0 and 1.

The above OKMC model only considers the temporal evolution of events. For the spatial evolution of events, we define it using the following schemes. The defects are described as spherical objects characterized by their compositions, shapes, center-of-mass, reaction radii, diffusion barriers, and binding energies. The details of the diffusion processes of objects are ignored and their diffusion are treated as jump events to the desired lattice sites. Vacancies and H atoms in the bulk diffuse randomly between the nearest body-centered cubic (bcc) sites and TIS sites with equal rate, respectively. The detailed diffusion mechanism is based on the atomic simulation and will be explained in the next section. Once a H moves towards a V or V cluster and their distance is less than the sum of the radius of these two objects, they can combine together and form a H_mV_n cluster. Meanwhile, a H atom has a certain

probability to be emitted from the formed cluster and the emitted H is randomly put at an nearest TIS site which is more than twice the sum of the radius of the two objects.

In order to describe the clustering behaviour of H and V, the OKMC model requires a complete parameter dataset of the H, V, and their clusters. These parameters include the pre-factor for migration probability, the migration energy (or diffusion barrier), the pre-factor for emission probability, the binding energy, and capture radius. These parameters are usually obtained from the atomic scale simulations or experimental results.

2.2. Parameterisation of vacancy clusters

The diffusion of V and V clusters is treated as they jump from one bcc lattice site to one of the eight 1st Nearest Neighbor (1NN) bcc lattice sites with the migration energy of 1.66 eV [22]. The binding energy of V to V1, V2, and V3 cluster is taken as 0.01, 0.19, and 0.78 eV, respectively, as reported by Heinola et al. [23]. For large V clusters, Becquart et al. [19] proposed a capillary approximation to estimate their binding energies. As for migration, the pre-factor P_0 of the migration probability is considered to be a function of V cluster size, and a migration energy of 1.66 eV is assumed for all V clusters. In the study of Castin et al. [16], the migration energies of various sizes V clusters were carefully studied. Results show that it is 2.77 eV for V clusters up to a size of 250. However, the H atom, with its migration energy of 0.20 eV, is quite similar to the case of SIA in Ref. [17], where SIA migration events are always selected by the MC algorithm due to its low migration energy, resulting in virtually frozen of vacancy defects. In this light, the V and V clusters are immobile in our simulation. The radius for a single V is 1.36 Å [24], and the radii for V clusters are given by an empirical expression related to the sizes of V_n clusters [19]. Impurities like carbon (C) atoms, are unavoidably present in W. As mentioned by Castin et al. [16], the technologically pure tungsten can have 200 appm or higher concentration of carbon. On the other hand, MD simulation results show that the H-C binding is very weak. The binding energies between H and C in the bulk W are in the range of 0.04-0.06 eV [25], which are far less than that of H with V around 1.20 eV [9]. Moreover, simulation results show that the existence of C atom in V has a minor effect on the binding energies of H and V, changing from 1.16 eV to 1.19 eV [25]. Therefore, the effect of carbon atoms on the trapping behaviors of H and V clusters can be ignored in this simulation.

2.3. Parameterisation of hydrogen diffusion

DFT calculations suggested that TIS is the energetically favourable site and the octahedral interstitial site (OIS) is the second energetically favourable site for H in W with a slightly difference of diffusion barrier of 0.29 eV [8]. Thus, there are two possible diffusion paths, TIS-TIS with a diffusion barrier of 0.20 eV and TIS-OIS-TIS with a diffusion barrier of 0.38 eV, for H in pure W [26]. However, Frauenfelder et al. [27] reported an experimental value of 0.39 eV for the diffusion barrier of H, which is higher than the DFT result [26]. Liu et al. calculated the diffusion coefficients of H in W at temperatures from 1900 K to 3000 K using molecular dynamics (MD) [28]. Their results showed that H atoms can be trapped by vacancies below 1900 K. And above 1900 K, V can still have a significant impact on H diffusion. Recently, Oda et al. [15] calculated the diffusion coefficients of H in W taking V into account by using an OKMC model with the diffusion barrier of 0.25 eV as an input parameter. They suggested that the diffusion barrier of 0.25 eV is a reasonable value and the higher experimental value of 0.39 eV may be caused by an over-estimation of the trapping influence by V. Considering the large effect of V on H diffusion, we use the diffusion barrier of 0.20 eV from DFT calculations and a pre-factor of 6×10^{12} s⁻¹ to describe the migration of H atoms between two adjacent TIS sites in our model. The clustering of H atoms is ignored due to the fact that the binding energy of two H atoms is only 0.02 eV at two 1NN TIS sites in W [26]. The capture radius for a single H atom is set as 3.0 Å [19].

2. 4 Parameterisation of hydrogen-vacancy clusters

The interaction of H with V has been widely discussed. Johnson and Carter [29] showed that a V₁ can trap six H atoms by taking the ZPE into account in calculating the binding energies. Recently, the binding energies of H to H_mV_n clusters were thoroughly investigated by Valles et al. [9] using the DFT method. They proposed a simple formula to estimate the binding energies of H_mV_n clusters as $E_b = 1.04$

× $(m/n)^{-0.43}$ for the process of $H+V \rightarrow H_{m-1}V_n$, where *m* and *n* is the number of H and V in the cluster, respectively. Note that this formula may be only accurate when the number of V is less than 5 since the formula is fitted to H_mV_{1-5} clusters. Using MS and four different potentials, Wang et al. [10] systematically investigated the interaction of H with V_{1-10} , then with V_{40} [11]. They obtained a logarithmic function of $E_b = \ln(c_1 + c_2 \times m)$ for the binding energies of the mth H, where c_1 and c_2 are fitting parameters. The radius of the H_mV_n cluster is assumed to be the same as that of the V_n cluster since the volume of the H atom is very small. In this work, we consider the sizes of vacancy clusters from V_1 to V_{40} in order to study the clustering behavior of H and V. The binding energies of H_mV_n clusters are listed in Table 1. The binding energies of H_mV_1 are taken from DFT results [8]. The binding energies of H_mV_{2-10} are taken from Ref. [10]. The binding energies of other $H_mV_{15,22,40}$ [11]. The calculation deails can be found in Section 3.1.

Cluster	E _b	Ref.
$H_mV_2 \left(H + H_{m-1}V_2\right)$	$ln(-0.2001 \times m + 3.4287)$	[10]
$H_{m}V_{3}(H + H_{m-1}V_{3})$	$ln(-0.1440 \times m + 3.4589)$	[10]
$H_mV_4 (H + H_{m-1}V_4)$	$ln(-0.1171 \times m + 3.5004)$	[10]
$H_{m}V_{5}(H + H_{m-1}V_{5})$	$ln(-0.0877 \times m + 3.2499)$	[10]
$H_mV_6 \left(H + H_{m-1}V_6\right)$	$ln(-0.0772 \times m + 3.3217)$	[10]
$H_mV_7 \left(H + H_{m-1}V_7\right)$	$ln(-0.0637 \times m + 3.2375)$	[10]
$H_mV_8 \left(H + H_{m-1}V_8\right)$	$ln(-0.0580 \times m + 3.2659)$	[10]
$H_{m}V_{9}(H + H_{m-1}V_{9})$	$\ln(-0.0570 \times m + 3.1999)$	[10]
$H_m V_{10} (H + H_{m-1} V_{10})$	$ln(-0.0568 \times m + 3.2114)$	[10]

Table 1. Binding energies (E_b) of H with H_{m-1}V_n clusters

$H_m V_{15} (H + H_{m-1} V_{15})$	$\ln(-0.0149 \times m + 3.1832)$	[11]
$H_m V_{22} (H + H_{m-1} V_{22})$	$\ln(-0.0248 \times m + 3.1749)$	[11]
$H_m V_{40} (H + H_{m-1} V_{40})$	$ln(-0.0330 \times m + 3.1139)$	[11]

The OKMC simulations presented in this work were performed using our in-house code. The simulation box was set as $100a_0 \times 100a_0 \times 100a_0$, where a_0 is the lattice parameter of W, 3.14 Å. All defects were randomly introduced in the simulation box. Each simulation was run for a enough long time to reach the equilibrium state of the system.

3. Results and discussion

In this section, we present the main OKMC simulation results with some relevant discussions. The determination of successive binding energies of H_mV_n clusters are presented first in section 3.1. Then in section 3.2, we show the effect of the temperature on the clustering behaviour of H with V or V clusters. Finally, we explore the effect of H concentration on the formation of H_mV_n clusters.

3.1. Determination of H successive binding energy with V clusters

A typical OKMC simulation requires a complete database for all kinds of defects that may occur during the simulation. In this work, to describe the traping behaviour of H with V_n (n = 1-30) clusters, the corresponding binding energies have to be pre-determined. Thanks to the DFT and MS simulations, successive binding energies of some H_mV_n clusters have already been obtained: the successive binding energies of H atoms to V_1 were obtained by DFT calculations [8]. For large clusters, by analyzing the MS simulation data, Wang et al. [10,11] found that the successive binding energies of H to H_mV_n clusters show a logarithmic relationship of $E_b = \ln(c_1 + c_2 \times m)$, where constants c_1 and c_2 are fitting parameters. In this work, we assumed that the binding energies of other H_mV_{11-40} clusters follow the same relationship, thus their binding energies can be determined based on this logarithmic relationship. The fitted binding energy of mth H atom to $H_{m-1}V_{15, 20, 30}$ cluster is determined to be ln(-0.0540 × m + 3.8000), ln(-0.0291 × m + 3.2520), and ln(-0.0286 × m + 3.7900), respectively. The calculated successive binding energies of H_mV_n clusters as a function of trapped H atoms are depicted in Fig. 1 (a). It can be seen from Fig. 1 (a) that the successive binding energies of H to $H_{m-1}V_n$ clusters decrease when the number of H atoms increases. Positive binding energies indicate the attraction of H with V or V clusters while negative ones indicate the repulsion of them. Thus, the intersection points between the curve of the number of trapped H and the zero binding energy give the maximum number of trapped H in V or V cluster. Accordingly, we also plot the maximum number of trapped H atoms in Fig. 1 (b).



Figure 1. (a) Number of trapped H in H_mV_n clusters for V₁₋₄₀ as a function of their binding energies. (b) Number and ratio of trapped H as a function of V clusters size at temperature of 0 K (black square). And the ratio of trapped H with the same V concentration (red triangles). Here the ratio *x_n* of trapped H is defined as N_{Vn}/N_{V1}, where N_{V1} is the number of total trapped H by V₁ and N_{Vn} is the number of total trapped H by V_n at 0 K.

In order to demonstrate the trapping ability of various V_n clusters for H atoms, we define a ratio of trapped H as $x_n = N_{Vn}/N_{V1}$, where n is the number of vacancies in the cluster, N_{V1} is the number of the total trapped H by V_1 , and N_{Vn} is the number of the total trapped H by V_n cluster. The results are given in Fig. 1(b). It clearly show that the trapping ability of V clusters to H drops dramatically with increasing of the number of V in clusters if the total amount of V is kept the same. For example, for the

 V_{30} cluster, the number of total trapped H drops by 40% compared with that for V_1 . We should point out, however, that all these results were obtained at temperature 0 K, and the effect of temperature will be investigated in the next section.

3.2. Effect of temperature on trapping of H by H_mV_n clusters

In this section, we studied the effect of temperature on the clustering behaviour of H with V_1 , V_2 , and large V clusters in W. Three temperatures of 300 K, 600 K, and 1000 K were used in our simulations. They correspond to three typical temperatures in fusion reactors. 300 K was considered as room temperature in our stimulation, while 600 K is the typical working temperature of the plasma facing materials [30–32]. The temperature of the tungsten divertor monoblock can be as high as 1000-2000 K estimated by simulations in Ref. [30–32], so 1000 K was considered as the high temperature in our stimulation.

3.2.1. Trapping behaviour of H by monovacancies

H atoms can be de-trapped from H_mV_1 clusters when the temperature is high enough. To study the effect of the temperature on the trapping behaviour of H by V clusters, we first simulated monovacancies with H atoms at three typical temperatures 300 K, 600 K, and 1000 K. The initial monovacancies and H atoms are randomly distributed in the simulation domain. Based on the DFT results [8], a monovacancy can trap up to 12 H atoms. The initial ratio of V to H was set to be 1:12, so its concentration is 30 and 360 atomic-parts-per-million (appm), respectively. The selected concentration of V is within the range of both simulation and experimental results. For example, several DFT stimulation results showed that the concentration of vacancy can vary from 0.1 appm to 1000 appm when H changes from 1 to 1000 appm. [33,34]. There are few experimental reports on the concentration V because of its difficulty to be measured directly. Xu et. al. [35] measured the post-irradiation V concentration to be 15-55 appm at the temperatures ranging from 300 K to 1000 K. In this work, we fix the vacancy concentration to be 30 appm for simplicity. We then perform a series of simulations to study the evolution of H_mV_1 clusters at various temperatures. For each temperature, the calculated fraction of

 H_mV_1 clusters as a function of time was obtained by averaging 20 separate simulation runs, where the random number seeds and initial positions of defects are varied in each simulation run.



Figure 2. Fraction of the H_mV₁ cluster as a function of time at temperatures of (a) 300 K, (b) 600 K, and (c) 1000 K, respectively. The fraction of the H_mV₁ cluster is defined as the ratio of number of H_mV₁ clusters with respect to the initial number of monovacancies.

Figure 2 shows the fractions of H_mV_1 (m = 1, ..., 12) clusters as a function of time at three temperatures. The fraction of H_mV_1 clusters is defined as the ratio of number of H_mV_1 clusters with respect to the initial number of monovacancies. It can be seen that the small H_mV_1 clusters form first and then continue to trap more H atoms to grow their sizes. After a certain time, stable H_mV_1 clusters are formed and their fractions are nearly independent on the time. Unstable H_mV_1 clusters disappear and their fractions approach to zero. Our simulations show the most stable cluster is H_8V_1 , H_6V_1 , and H_5V_1 at 300 K, 600 K, and 1000 K, respectively, whereas the DFT calculations [8] indicate that a single vacancy can trap up to 12 H atoms. This means that the trapping behaviour of H by the monovacancy is significantly affected by temperature. The reason can be attributed to the increased de-trapping probability of H from the H_mV_1 clusters at high temperature. For the temperature of 300 K, the most stable cluster is H_8V_1 , H atoms can be easily emitted from $H_{9,12}V_1$ clusters because their binding energies are close to zero. Thus, $H_{9,12}V$ clusters disappear and H_8V clusters are stabilized. At 600 K, H_6V_1 is the most stable cluster. All other H_mV_1 clusters disappear. For the temperature of 1000 K, four clusters

including H_3V_1 , H_4V_1 , H_5V_1 , and H_6V_1 are stable. Among them, H_5V_1 has the largest volume fraction. At 300 K, all H atoms are trapped in H_8V_1 clusters, while the number of trapped H atoms drops to about 50% at 1000 K. This is because the binding energies of H_mV_1 with H atoms continuously decrease with H_mV_1 trapping more H atoms. The last trapped H atoms are thus very unstable due to their relatively small binding energies. With increasing temperature, those H atoms can be easily de-trapped from the H_mV_1 clusters and become mobile interstitials in W. Comparing with our previous results that used the binding energies without considering the ZPE [18], we find that the number of H atoms trapped by H_mV_1 clusters decreases for all temperatures when the ZPE is taken into account. For example, at 300 K the size of H_mV_1 drops from $H_{10}V_1$ (without ZPE) to H_8V_1 (with ZPE), at 600 K from H_9V_1 (without ZPE) to H_6V_1 (with ZPE), and at 1000 K from $H_{5-7}V_1$ (without ZPE) to $H_{4-6}V_1$ (with ZPE). The required time for reaching the equilibrium of the system is largely dependent on temperature. It is about 10 microseconds at 300 K, while it is around 25 nanoseconds at 1000 K. This is because the possibilities of events increase at high temperature, which shorten the time of the events based on Eq. (2).



Figure 3. Fraction of the H_mV_1 cluster as a function of the number of trapped H at temperatures ranging from 300 K to 1000 K. The fraction of the H_mV_1 cluster is defined as the ratio of number of the H_mV_1 clusters with respect to the initial number of V.

Figure 3 shows the fractions of H_mV_1 clusters as a function of the number of trapped H by monovacancies at temperatures ranging from 300 K to 1000 K. It can be seen that the number of trapped H atoms by monovacancies decreases with the increase of temperature, which is consistent with previous results [34,36]. As expected, more H atoms are emitted at high temperatures than at low temperatures.

3.2.2. Trapping behaviour of H by di-vacancies

With the same conditions as above, we further examined the effect of temperature on the clustering behaviour of H atoms with di-vacancies. For the purpose of comparison, the concentrations of H and V are set as the same as previous simulations used. Thus, the number of di-vacancies in this new set of simulations is exactly half number of the mono-vacancies in the previous calculations. Figure 4 shows the fractions of H_mV₂ clusters as a function of time. In general, the fractions of H_mV₂ clusters exhibit similar trends as shown in Fig. 2. Small H_mV₂ clusters form first, and then they attract more H atoms to grow to large H_mV₂ clusters. The most stable H_mV₂ clusters obtained are H₁₁V₂, H_{9,10}V₂, and H_{7,8,9}V₂ at 300 K, 600 K, and 1000 K, respectively, which clearly indicates that the trapping ability of H_mV₂ decreases with increasing temperature. According to the binding energies of mono-vacancies obtained from DFT and di-vicancies from MS calculations, both of which can trap 12 H. As a result, more H atoms remain mobile for the case of di-vacancies than the ones for mono-vacancies at the same temperature.



Figure 4. Fraction of the H_mV_2 cluster as a function of time at temperatures of (a) 300 K, (b) 600

K, and (c) 1000 K, respectively. Fraction of the H_mV_2 cluster is defined as the ratio of number of the

H_mV₂ cluster with respect to the initial number of di-vacancies.

A more detailed information on H_mV_2 clusters at temperatures ranging from 300 K to 1000 K is given in Fig. 5. As the temperature increases, more stable H_mV_2 clusters have a smaller number of H atoms. Furthermore, the fraction of H atoms outside H_mV_2 clusters increases with increasing temperature.



Figure 5. Fraction of the H_mV₂ cluster as a function of temperatures ranging from 300 K to 1000 K. Fraction of the H_mV₂ cluster is defined as the ratio of number of the H_mV₂ clusters with respect to the initial number of V.

3.2.3. Trapping behaviour of H by large V clusters

Formation of V clusters is often observed in irradiated W in experiments. For example, Eleveld et al. [37] observed stable V_{11-16} clusters after heating at 650 K for the 30 keV D_2 ion irradiated samples at room temperature. Ferroni et al. [38] reported a similar observation of V clusters in W irradiated with 2

MeV W ion. We then study the clustering behaviour of H atoms with V clusters. Different initial Vn clusters size of n = 1-30 are used and their initial concentrations (C_V) are set as 30 appm. The initial H concentration (C_H) is set as C_v multiplied by the number of maximum trapped H atoms at 0 K (N_{Vn}^{0}) for each cluster, which has an expression of $C_V \times N_{Vn}^{0}$. Figure 6 shows the average number of trapped H atoms as a function of temperature for six selected V clusters. The average number of trapped H atoms in V clusters decreases with the increase of temperature for all cases. This is due to the increased detrapping probabilities with temperature. The average number of trapped H atoms for each type of V clusters is almost proportional to temperature except for mono-vacancies. For mono-vacancies, the binding energies of H₆V₁ clusters with H atoms are only about 0.2 eV according to DFT calculations [8]. Thus, the $H_{7-12}V_1$ clusters are very unstable and H atoms can be easily de-trapped with increasing temperature, resulting in stable clusters H_8V_1 at 300 K, H_6V_1 at 600 K, and H_6V_1 at 1000 K. When the size of the V clusters increases, the average number of trapped H atoms in V clusters decreases largely for small V clusters but changes slightly for large ones. For example, clusters V₁₀, V₁₅, V₂₀, and V₃₀ can trap three H atoms at 300 K and two H atoms at 1000 K. Thus, we can expect that the average number of trapped H atoms around three H atoms at 300 K and two H atoms at 1000 K with the size of V clusters is larger than 30.



Figure 6. Average number of trapped H atoms by V_{1, 5, 10, 15, 20, 30} clusters as a function of temperature of 300 K, 600 K, and 1000 K.

3.3. Effect of H concentration and V cluster size on the clustering

The initial H concentration can have a great impact on the clustering behaviour of H_mV_n . To study the effect of H concentration on the clustering of V, we performed a series of simulations with varing the H concentration from 50 to 1000 appm. The initial V_n clusters are randomly distributed in the simulation box with the same concentration of V for all V_n cases. Our study suggests that the maximum number of H captured by vacancy defects increases rapidly when the concentration of H is low, but reaches an equilibrium value with further increasing the H concentration. By setting the initial H concentration above the equilibrium value, we can study the effect of vacancy size on the clustering behaviors of H_mV_n clusters.

3.3.1. Effect of H concentration on the clustering of $H_m V_n$

A series of simulations of selected V clusters with different initial H concentrations have been carried out at temperatures of 300 K, 600 K, and 1000 K, respectively. In order to demonstrate how many H atoms are trapped by V clusters, we define the fraction of trapped H atoms as $p_n = N_{Vn}^{T}/N_{V1}^{0}$, where $N_{Vn}{}^{T}$ is the average number of trapped H by each V_n at the temperature of the simulation, and $N_{V1}{}^{0}$ is the total number of trapped H by V_1 predicted by MS at 0 K. The calculated fractions of trapped H atoms as a function of the initial H concentration are shown in Fig. 7. Generally, the fraction of trapped H atoms increases when the H concentration increases at the beginning. It then changes gradually after the initial H concentration is larger than 250 appm for 300 K, 500 appm for 600 K, and 2000 appm for 1000 K, respectively. This suggests that the effect of the initial H concentration for a long time evolution can be ignored when the initial H concentration is large enough. For each temperature, the maximum concentration of trapped H decreases when the sizes of V clusters increase, according to their binding energies. Specifically, at 300 K, the fraction of trapped H for V_1 increases rapidly when the initial concentration of H increases and then reaches a steady state after the H concentration reaches 1000 appm. V₂₋₅ and V_{10,15,20,30} reach their equilibrium states quickly after 250 appm and their trapped H fractions are 40% and 30%, respectively. At 600 K, when the concentration of H is larger than 500 appm, the fraction of trapped H is about 50% for V_1 while it is about 35% for V_{2-5} and 25% for $V_{10,15,20,30}$. At 1000 K, the fraction of the H concentration for H_mV_1 is about 40%, and for all other V clusters it is around 20-30%. In general, the fraction of trapped H is large for the H_mV_n clusters which contain little vacancies (i.e. small n). It is also expected that the maximum number of trapped H atoms decreases when the temperature increases due to the increased probability of H emission. Therefore, the H saturation concentration for each V cluster has to be estimated for all temperatures.



Figure 7. Fraction of trapped H atoms x as a function of the initial H concentration at 300 K (a), 600 K (b), and 1000 K (c). The fraction of trapped H atoms is defined as N_{Vn}^T/N_{V1}⁰, where N_{Vn}^T is the average number of the trapped H for each V_n at elevated temperature, and N_{V1}⁰ is the number of the total trapped H by V_n predicted by MS at 0 K.

3.3.2. Effect of the V cluster size on the clustering of $H_m V_n$

With the determination of the H saturation concentration as shown in Fig. 7, we then study the effect of the V cluster size on the clustering behaviour of H_mV_n under H saturation condition. Thus, the effect of H concentration on the clustering of H_mV_n is considered to be very small. For this study, the initial H concentration is set to be 2000 appm, and the initial concentration of V clusters is 30 appm. Three different temperatures of 300 K, 600 K, and 1000 K were chosen. Figure 8 shows the average number of trapped H atoms as a function of temperature for six selected V clusters with saturated H concentration and, as a comparison, with unsaturated H concentration (same as the results presented in Fig. 6). For a particular size of V_n cluster, the number of trapped H atoms decreases when the temperature increases. This can be explained by the fact that the high temperature can increase the possibilities of H de-trapping events. The average number of trapped H atoms in the saturated H concentration case is much larger than the one in the unsaturated case for a fixed size of V_n clusters. This is because V_n clusters can trap as many H atoms as possible when a enough concentration of H is provied. As a consequence, every V_n cluster will be filled with H atoms. Larger V_n clusters can trap more H atoms on average since they have more rooms. Furthermore, for the saturated H concentration case, the average number of trapped H atoms in V clusters increases when the size of V clusters increases, in contrast with the unsaturated case as shown in Fig. 6. The reason is that larger V clusters can accommodate more H atoms than smaller V clusters when the saturated H concentration is provided. However, for the unsaturated H concentration case, the number of large V clusters is less than the number of small V clusters (as we assumed the total amount of V to be the same). Thus, the small number of large V clusters reduces the probability of forming H_mV_n clusters when the H concentration is limited, which leads to the fact that the average number of trapped H atoms in V clusters decreases when the size of V clusters increases.



Figure 8. Average number of trapped H atoms by V₁, _{5, 10, 15, 20, 30} clusters as a function of temperature of 300 K, 600 K, and 1000 K.

The calculated fractions of trapped H atoms as a function of V_n size are shown in Fig. 9. The fraction of trapped H atoms is defined as the ratio of trapped H atoms with respect to the total number of H atoms. For a given temperature, the number of trapped H decreases when the sizes of V_n clusters increase. It then changes gradually after n = 10, which implies that the trapping capability of H_mV_n clusters to H atoms decreases with the increase of the sizes of H_mV_n clusters. Thus, compared to the trapping behaviour of H_mV_n with H atoms with the unsaturated H concentration in Fig. 6, the clustering behaviour of H_mV_n is mainly determined by the sizes of V clusters when the saturated H concentration is reached.



Figure 9. Fraction of trapped H atoms as a function of the vacancy size at three different temperatures of 300 K, 600 K, and 1000 K.

3.3.3 Discussion

At present, it is still a big challenge to estimate the H retention in irradiated W from experimental or simulation approaches [39]. The total H retention in W is a very complex phenomenon as it is impacted by many factors such as manufacturing processes, impurities, temperatures, energy and flux of incident H, and irradiated defects. Thermal desorption spectroscopy (TDS) is the main experimental technical

tool to study the H retention in W. Based on the TDS peak of the desorption flux, various trapping energies and trapping sites of H can be obtained [40–43]. Experimental measurements [44–46] of diffusion coefficients of H in W show that H can be easily released once dissolved in W at high temperature, which means that most H atoms remaining in W are trapped and immobilized above room temperature. Thus, it is of a particular interest to determine how many H atoms can be trapped in W. However, there are many types of trapping sites in the irradiated materials and those can be intrinsic/extrinsic defects, impurities and surface impurities, and so on. Considering all of them together in a single simulation seems to be impractical. In the present work, we apply the OKMC method to study the trapping behaviour of H_mV_n clusters to H atoms by varying temperature, size of clusters, and H concentration. The number of trapped H atoms in V clusters is determined by balancing the trapping process and dissociation process. We find that the retention of H atoms in W is, as expected, dependent on the state of the trapping sites and temperature. Further studies are needed to explore the effects of the grain boundary, dislocation, and impurity atoms on the H retention in W.

4. Conclusions

We have studied the clustering behaviour of hydrogen (H) with vacancy (V) clusters in tungsten (W) by using Object Kinetic Monte Carlo (OKMC). The results show that the temperature and sizes of V clusters can have significant influences on the interaction of H atoms with V clusters. The maximum trapped H atoms in monovacancy decreases when the temperature increases, which is 8, 6, and 5 at 300 K, 600 K, and 1000 K, respectively, and largely different from the atomic simulation results obtained at 0 K. The reason can be attributed to the increased emission probability of H atoms at high temperature. When the sizes of V clusters increase, their trapping abilities significantly drop if we assume the total amount of V to be the same. This is due to the binding energies of H_mV_n clusters decrease gradually as the number of trapped H atoms increases. For the case of the given saturated H concentration, the average number of trapped H atoms is much larger than the one in the unsaturated case for identical V cluster sizes. This is due to the V_n clusters that can trap as many H atoms when the H concentration is

saturated. The average number of trapped H atoms in V clusters in the saturated case increases with increasing sizes of V clusters, which is in contrary to the one in the unsaturated case. To conclude, the trapping behavior of V_n clusters in saturated H concentration is largely different from that in unsaturated conditions and is mainly determined by the sizes of vacancy clusters. Our final goal is to integrate more irradiated defects into the OKMC model, and to understand the H retention under irradiation. We believe that the present simulations can provide useful references for understanding the clustering of H and V in W.

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