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# Experimental Study and DEM Simulation of Size Effects on the Dry Density of Rockfill Material

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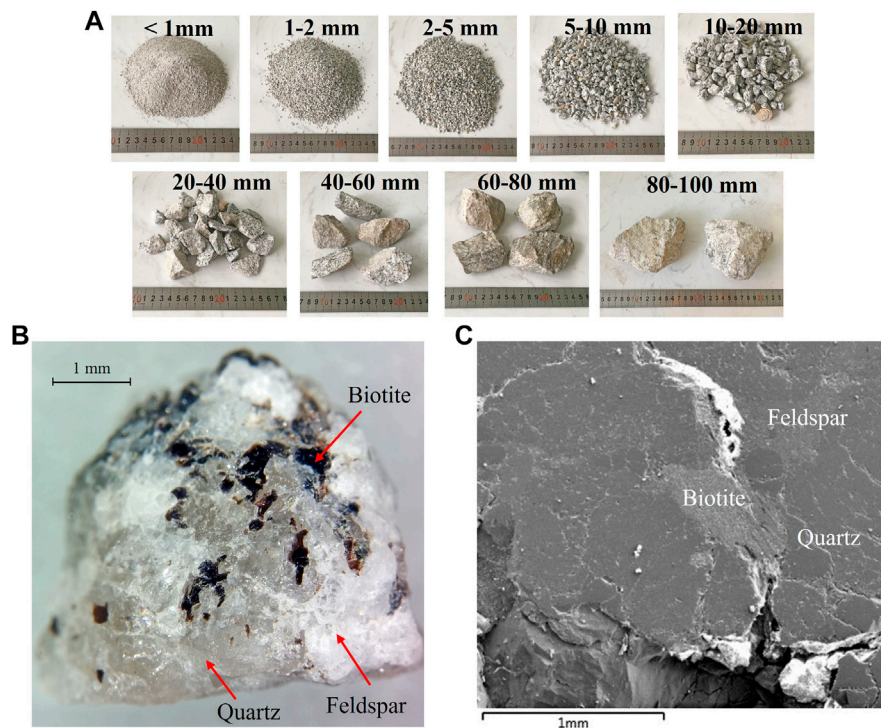
The initial dry density has a significant effect on the mechanical behavior of rockfill material (RFM). The size effects on the minimum/maximum dry density (referred to as dry density,  $\rho_d$ ) of RFM still need further study. To investigate the relationship between  $\rho_d$  and  $d_M$ , a series of surface vibration compaction tests and DEM simulations are performed on the samples with different maximum particle sizes  $d_M$ . Both the physical and numerical results exhibit that  $\rho_d$  increases fast when  $d_M$  ranges from 10 to 40 mm. When  $d_M$  exceeds 40 mm,  $\rho_d$  increases slowly and tends to be a constant. Results indicate that  $\rho_d$  is affected by the gradation. To consider the gradation effect, a normalized parameter  $\lambda$  is introduced, and the relation between  $\rho_d$  and  $d_M$  can be characterized by an empirical equation.

**Keywords:** rockfill material, maximum dry density, compactability, gradation, surface vibration test, particle size, discrete element modeling

## 1 INTRODUCTION

Rockfill material (RFM) has been widely used in the construction of dams and railway embankments due to its inherent flexibility, capacity to cope with large seismic actions, and adaptability to various foundation conditions. Nowadays, the maximum diameter  $d_M$  of rockfill particles used in the field can be up to 1,200 mm [1]. However, the  $d_M$  allowable in laboratory is usually not more than 60 mm because of the limitation of apparatus size [2]. Therefore, several scaling techniques have been proposed to prepare the scaled samples. The scaling techniques include the scalping technique [3], the parallel gradation technique [4], the quadratic grain size distribution technique [5], the replacement technique [6], the hybrid method [7, 8], etc. Although the scaling techniques have been widely applied, the size effects on the properties of RFM have still not been fully understood [9–11].

Many researchers have studied the size effects on the mechanical behavior of RFM via large-scale triaxial tests [1, 12–14]. However, most of the studies neglect the size effects on the density of rockfill samples. Limited literature on the size effects of density can be found [15, 16]. Experimental results show that the mechanical behavior of RFM is directly related to its initial density (or void ratio) [17, 18]. Hence, the size effects on the density of RFM need further investigation. In contrast, the discrete element method (DEM) is a good tool to simulate granular materials because of their discontinuous and heterogeneous natures [19]. In practice, the DEM has been widely used to reproduce the laboratory tests on granular materials (e.g., soil, sand, and RFM) [20–22]. The responses of the granular materials can be understood in the particle scale.



**FIGURE 1** | Macroscopic observations on (A) Shuangjiangkou rockfill particles of sizes 1–100 mm. Microscopic observations on Shuangjiangkou rockfill particles: (B) surface view with different mineral compositions; (C) FE-SEM image of one typical rockfill particle.

Generally, the minimum dry density  $\rho_{d,min}$ /maximum dry density  $\rho_{d,max}$  (referred to as dry density,  $\rho_d$ ) is mainly controlled by the gradation and particle shape [23–28]. There are few analytical models for predicting the minimum/maximum dry densities. Kezdi [29] proposed an analytical method to estimate the  $\rho_{d,max}$  of sand-silt mixtures. The method is based on the ideal situation that the void space among sand grains can be effectively filled by silt particles without altering the packing structure of sand. Hence, this method usually overestimates the realistic  $\rho_{d,max}$  [30]. In combination with the liquefaction potential of silty sand, Lade et al. [31] also proposed a formula to predict the  $\rho_{d,max}$ . The formula is also based on the ideal situation used by Kezdi [29] and thus overestimates the  $\rho_{d,max}$ . Korfiatis and Manikopoulos [32] proposed a piecewise linear relationship between the particle size distribution (PSD) curve and the  $\rho_{d,max}$  of granular soils based on the theoretical formulations. The basic assumption in the model is that the log-normal gradation is expected to be a straight line and is determined by two parameters, i.e., a center point and a slope. Chang et al. [33] also proposed an analytical method for predicting the  $\rho_{d,max}$  of sand-silt mixtures. The analytical methods mentioned here have been focused on sand-silt mixtures. Therefore, these models can not be applied to soils with a wide range of particle sizes, like RFM.

In this study, the size effects on the dry density of RFM are investigated by a series of surface vibration compaction tests and numerical simulations. The relationship between  $\rho_d$  and  $d_M$  is

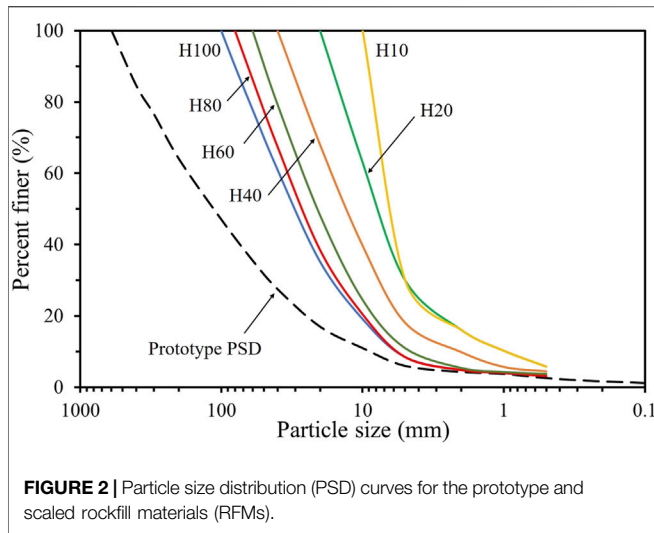
discussed. An empirical equation is proposed to describe the relation between  $\rho_d$  and  $d_M$  considering the effect of gradation.

## 2 EXPERIMENTS

### 2.1 Test Materials

The studied materials were obtained from the Shuangjiangkou rockfill material resources field in western China. The rockfill particles of sizes from 1 to 100 mm are shown in **Figure 1A**. The rock is a granite mainly composed of feldspar, quartz, and biotite, with an angular/sub-angular shape (as shown in **Figure 1B**). Field emission scanning electron microscope (FE-SEM) and energy-dispersive X-ray spectroscopy (EDS) were used to identify the mineral compositions (**Figure 1C**). The specific gravity of rockfill particles is 2.68. The  $d_M$  of the studied RFM is 600 mm, which is greater than the limit of the conventional test apparatus in laboratory. Therefore, the prototype gradation of RFM should be scaled down by scaling techniques.

The hybrid method [7, 8] is adopted in the present study. In practice, it is a combination of the parallel gradation and replacement techniques. The method is popular in China as it has both the advantages of these two scaling techniques. In this method, the gradation is first scaled parallelly by an appropriate ratio to ensure that the percentage of fine fraction (i.e.,  $d < 5$  mm) is less than 30%. After that, if the oversized fraction (i.e.,  $d > d_M$ ) still remains, it will be replaced proportionally by the coarse



fraction (i.e.,  $5 \text{ mm} < d < d_M$ ). As a result, the scaled gradation curve has a similar shape compared to the prototype, and the content of fine fraction is also limited to a low value.

Six different values of  $d_M$  (10, 20, 40, 60, 80, and 100 mm) are adopted for the dry density tests. The chosen values of  $d_M$  are in the range of the commonly used maximum particle sizes in laboratory. In practice, the diameter of triaxial samples can be 61.8, 101, and 300 mm while the maximum particle size allowable is 1/5 of the sample diameters [7, 8, 34], i.e., 10, 20, and 60 mm.

The particle size distribution (PSD) curves for prototype and scaled RFMs are shown in **Figure 2**. The PSD curves are labeled by the letter H and a number. The letter H represents the hybrid method and the number indicates the value of  $d_M$ . Prior to the usage in the experiment, the soil is sieved into different fractions, and each individual fraction is then mixed according to the given PSD to prepare laboratory samples. In the dry density tests, the specimen is not divided into layers before compaction.

## 2.2 Dry Density Tests

The  $\rho_{d,min}$  (or maximum void ratio  $e_M$ ) is obtained by the loose-fill method [8, 35]. The  $\rho_{d,max}$  (or minimum void ratio  $e_m$ ) is determined using the surface vibration compaction test [8, 36].

The surface vibration test device includes a steel mold, a steel plate, and a surface vibrator. The steel mold (diameter 303 mm and height 418 mm) is used to hold the soil samples. The surface vibrator has an exciting force of 4.2 kN with a motor frequency of 50 Hz and an amplitude of 2 mm. The steel plate is positioned on the top of the sample to ensure a uniform distribution of vertical stress applied to the samples. The steel plate is 280 mm in diameter and 20 mm in height. The static pressure applied on the samples by the vibration hammer is 14 kPa.

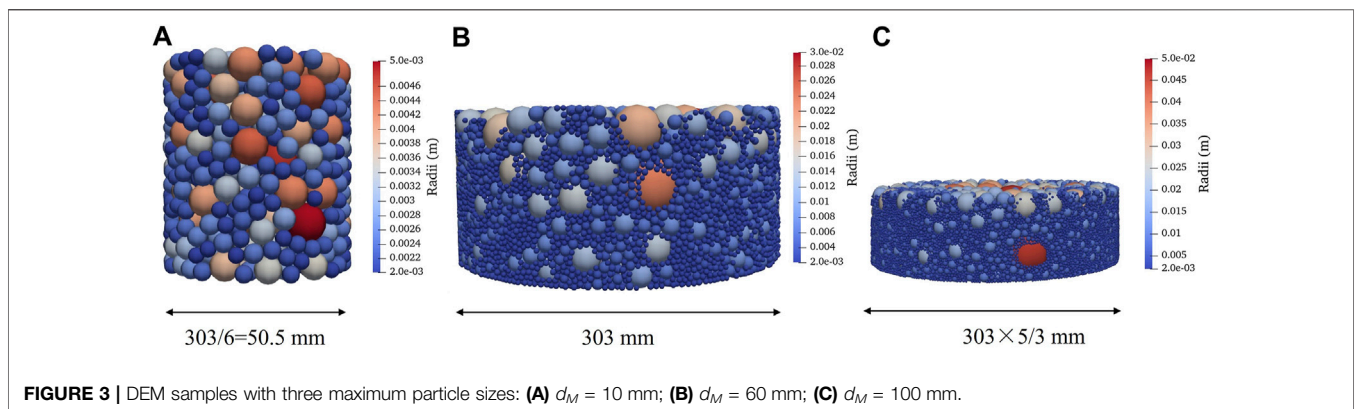
In the loose-fill method, the soil sample is filled into a container by using a small shovel. To ensure that the soil sample slowly slides into the container, the small shovel should touch close to the surface of soil during filling. The filling process is stopped until the filled soil is above the top of the container. The top surface of the container is then leveled by the shovel, and the weight of the container and soil sample is measured. Then, the  $\rho_{d,min}$  can be obtained. In the surface vibration test, a soil sample of 40 kg are carefully prepared and filled into the steel mold by the small shovel. The steel plate is then placed on the surface of the sample, on which the surface vibrator is placed. The vibration time is 15 min for the densest state. The  $\rho_{d,max}$  can then be determined by measuring the sample height. The tests are repeated two times and an average value is adopted for a more reliable result.

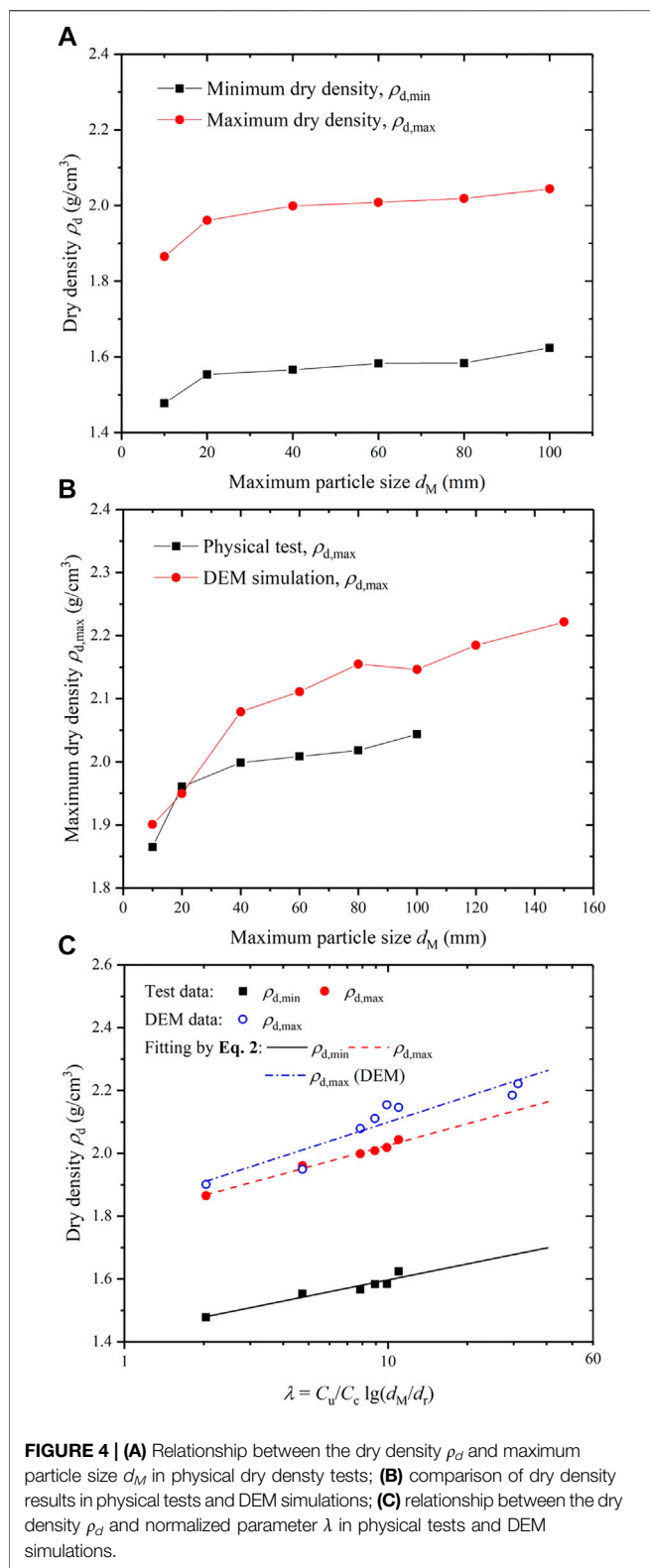
## 3 NUMERICAL MODELING

### 3.1 DEM Modeling of Rockfill Material

To better understand the size effects on the  $\rho_{d,max}$  of RFM, a series of DEM simulations of dry density tests are conducted. The DEM is performed by YADE, an open source framework [37]. The particles are generated according to the PSD curves in **Figure 2**. For the samples with  $d_M = 120 - 150$  mm, the parallel gradation technique is used for scaling. For a compromise between the computational efficiency and a relatively realistic reconstruction of samples, the fine fractions (i.e.,  $d < 5$  mm) are all replaced by particles with size  $d = 5$  mm.

The rigid container for holding the sample with  $d_M = 60$  mm is 303 mm in diameter and 600 mm in height. For the rest of samples with a given  $d_M$ , the corresponding container diameter and height are scaled by a factor  $f = d_M/60$  to ensure





the same sample-size ratio (SSR), which is the ratio of the sample diameter to  $d_M$  [38–40]. The rigid container is constructed by rigid facet units. Linear contact model [19] in DEM is used with

the Young’s modulus of 60 MPa and Poisson’s ratio of 0.45. Both the friction angles of walls and balls are 0, i.e., the friction angles of all contacts are set as 0 for a dense state of soil samples. The density of particles is 2.68 (g/cm<sup>3</sup>). No calibration is made here, and the model parameters are chosen considering an appropriate computational time. The aim of the DEM simulation is to provide more data for the study of relationship between  $\rho_{d,max}$  and  $d_M$ . The  $d_M$  is not more than 100 mm in physical tests due to the limitation of apparatus size, while the  $d_M$  can be up to 150 mm in DEM simulation. Typical numerical samples with  $d_M = 10$  mm, 60 mm, and 100 mm are given in **Figure 3**.

### 3.2 Simulation of Compaction Process

In the physical tests, the dense soil samples are obtained by surface vibration tests. However, a dense sample in DEM can be easily obtained by setting the friction angle as 0 [41, 42], which is adopted in the present study. The particles are first deposited into the container under gravity. After that, a rigid wall is generated above the sample and then moved downward until a vertical pressure of 14 kPa is reached. The pressure of 14 kPa is same to the static pressure applied by the vibration hammer in physical tests. The simulation is terminated when a steady state is reached.

## 4 RESULTS AND DISCUSSION

**Figure 4A** shows the relationship between the  $\rho_d$  and  $d_M$  in the physical dry density tests. Both the  $\rho_{d,min}$  and  $\rho_{d,max}$  increase with the increase of  $d_M$ . The  $\rho_d$  increases rapidly when  $d_M$  ranges from 10 to 40 mm. When  $d_M$  exceeds 40 mm, the  $\rho_d$  increases slowly and tends to be a constant. These results can be explained by the gradation: with a wide range of particle sizes, the sample with a large  $d_M$  is better graded than that with a small  $d_M$ . This observation is consistent with the previous laboratory test results [27, 40, 43, 44].

**Figure 4B** shows the comparison of the  $\rho_{d,max} - d_M$  relations in physical tests and numerical simulations. The  $\rho_{d,max} - d_M$  relation in the physical tests can be generally reproduced by the DEM simulations: the  $\rho_{d,max}$  increases fast when  $d_M$  ranges from 10 to 40 mm and then increases slowly and tends to be a constant. The high value of  $\rho_{d,max}$  in DEM simulation should be partly attributed to the chosen assumptions (spherical particle and friction angle of 0). The use of complex particle shapes and non-zero friction angles would be more faithful to the facts. However, the choice of friction angle of 0 and spherical particles in the present study is in consideration of computational time. In DEM, the bonded particle model (BPM) or polyhedron is used to describe the irregular particle shape. The BPM needs many elementary balls to generate an agglomerate [45], and the polyhedron needs complex contact detection methods [46]. The effect of particle shape on the  $\rho_d$  has been seldom studied by DEM. Jensen et al. [47] used a 2D BPM to study the effect of particle shape on the void ratio. They confirmed that the void ratio of a particle mass increased as the angularity or roughness of the particle increased. Deng et al. [45] used a 3D BPM to simulate the dynamic process of particle packing with different particle aspect ratios. The above studies verify the important effect of particle shape on  $\rho_d$ . However, the numerical samples reported in the

literature are usually uniformly graded, and the particle packing with a wide gradation is not considered due to the high computational cost.

Based on the work of Zhu et al. [48], the normalized parameter  $\lambda$  can be used to describe the relationship between dry density, gradation, and maximum particle size, which can be expressed as

$$\lambda = C_u/C_c \lg(d_M/d_r) \quad (1)$$

where  $C_u$  = coefficient of uniformity,  $C_c$  = coefficient of curvature,  $d_r = 1$  mm, i.e., reference size. The maximum particle size  $d_M$  is the value of maximum particle size in a PSD. The  $C_u$  and  $C_c$  are defined as [49]

$$C_u = d_{60}/d_{10} \quad (2)$$

$$C_c = d_{30}^2 / (d_{10} \times d_{60}) \quad (3)$$

where  $d_{10}$ ,  $d_{30}$ , and  $d_{60}$  are the particle diameter corresponding to 10, 30, and 60%, respectively, passing on the cumulative PSD curve. Therefore, the values of  $C_u$  and  $C_c$  are related to the width and shape of PSD curve. The relationship between  $\rho_d$  and  $\lambda$  is given in a semi-logarithmic scale (Figure 4C). The data points can be well fitted by a linear function

$$\rho_d = \rho_w (a \lg(\lambda) + b) \quad (4)$$

where  $a$  and  $b$  are the fitting parameters;  $\rho_w$  is the density of water, 1 g/cm<sup>3</sup>. In the present study,  $a$  and  $b$  are 0.10 and 1.80, 0.07 and 1.43, for the  $\rho_{d,max}$  and  $\rho_{d,min}$  of the studied RFM, respectively. For the prototype gradation (i.e.,  $d_M = 600$  mm,  $C_u = 19.61$ ,  $C_c = 1.35$ ,  $\lambda = 40.4$ ), the  $\rho_{d,max}$  and  $\rho_{d,min}$  are estimated to be 2.164 and 1.700 g/cm<sup>3</sup> by Eq. 4, increasing by 7.74 and 7.37% compared to the corresponding value of H60 sample, respectively.

DEM simulation results are also illustrated in Figure 4C. The data points can also be linearly fitted, shown as a dash-dotted line. The applicability of Eq. 4 has been verified by the numerical simulation when the  $d_M$  is in the range of 10–150 mm.

## 5 CONCLUSION

The size effects on the minimum/maximum dry density (referred to as dry density,  $\rho_d$ ) of rockfill material are

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studied by a series of surface vibration compaction tests and DEM simulations. Both physical and numerical results show that the  $\rho_d$  increases fast when the  $d_M$  ranges from 10 to 40 mm and then increases slowly and tends to be a constant. By introducing the nominal parameter  $\lambda$ , an empirical equation is proposed to describe the relation between  $\rho_d$  and  $d_M$  considering the effect of gradation. A more accurate predictive formula considering particle shape needs further investigation. This study can provide a valuable reference to understand the size effects on the dry density of rockfill material.

## DATA AVAILABILITY STATEMENT

The original contributions presented in the study are included in the article/Supplementary Material, further inquiries can be directed to the corresponding authors.

## AUTHOR CONTRIBUTIONS

Funding acquisition and formal writing of the work, XZ and JZ; investigation and data analysis of the work, XZ, YW, and NB; review and editing of the work, JZ, YJ, J-BC, and HB. All authors have read and agreed to the published version of the manuscript.

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